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Abstract: The Cloud Imaging and Particle Size (CIPS) instrument on the AIM spacecraft is a 4-camera nadir pointed imager with a bandpass centered at 265 nm and a field of view of 120 by 80 degrees. CIPS observes Polar Mesospheric Clouds (PMCs) against the sunlit Rayleigh-scattered background. At individual polar locations approximately 5 by 5km in area, CIPS observes the same volume of air seven times over a range of scattering angles from about 35 to 150 degrees. These multi-angle observations allow the identification and extraction of the PMC scattered radiance from the Rayleigh-scattered background. We utilize the fact that the former has a highly asymmetric phase function about 90° scattering angle, while the latter has a phase function that is symmetric. The retrieved PMC phase function can then be interpreted to obtain PMC particle size distributions. We describe a technique for identification of PMCs in the CIPS observations through the separation of the Rayleigh and PMC radiances. PMC phase function results are shown for the first season of CIPS observations. Assuming the particles are oblate spheroids with an axial ratio of 2, and a Gaussian distribution of width 14 nm, we find the phase functions are consistent with mean radii between 50 and 60 nm. These results are similar to those discussed by Hervig et al. [2008] in this issue from the Solar Occultation for Ice Experiment (SOFIE) which also flies on the AIM satellite.

1 **Phase Functions of Polar Mesospheric Cloud Ice as Observed by the**
2 **CIPS Instrument on the AIM Satellite**

3

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12 **Abstract**

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14 nadir pointed imager with a bandpass centered at 265 nm and a field of view of 120 by 80
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28 also flies on the AIM satellite.

29 **1.0 Introduction**

30 Polar Mesospheric Clouds (PMCs) are a high-latitude, summertime phenomenon that has
31 generated significant interest in recent decades. PMCs were first observed in 1885 [Leslie, 1885]
32 and there is evidence that their brightness and frequency of occurrence have been increasing
33 since at least 1979 [Shettle et al., 2002; DeLand et al., 2003; 2007]. Hemispheric differences in
34 their spatial and temporal morphology have been found [see Bailey et al., 2007 and references
35 there in]. Evidence for control of their morphology by solar forcing [DeLand et al., 2007],
36 geomagnetic forcings [von Savigny et al., 2007], lower atmosphere meteorology [Berger and
37 Leubken, 2006], and winter hemisphere stratospheric dynamics [Karlsson et al., 2007] have also
38 been shown. It has been suggested (and debated) that increases in their occurrence frequency and
39 brightness are linked to global change [Thomas 2003, see also von Zahn, 2003 and Thomas et
40 al., 2003]. A complete understanding of the variability of PMCs and any potential link to climate
41 change is hindered by an incomplete understanding of the microphysics of these clouds [Rapp
42 and Thomas, 2006].

43 The scattering phase function of PMC ice is an important quantity for understanding PMC
44 microphysics. The phase functions are directly related to the size distribution, index of refraction,
45 and shape of the ice particles [Rapp et al., 2007]. Although only a limited number of space
46 based-observations of PMC scattering phase functions exist [Gumbel et al., 2001], bidirectional
47 observations of PMCs by the Student Nitric Oxide Explorer [SNOE, Bailey et al., 2005] and the
48 Solar Mesosphere Explorer [SME, Thomas, 1984] have inferred some information about the
49 PMC phase function and utilized it to infer particle sizes [Thomas and McKay, 1985; Rusch et
50 al., 2008]. In this work we describe the first satellite observations of PMC ice phase functions.

51 The Cloud Imaging and Particle Size (CIPS) instrument on the Aeronomy of the Ice in the
52 Mesosphere (AIM) satellite was designed to image PMCs from space and to determine their ice
53 scattering phase function at high spatial resolution (~ 5 km) over the summer polar cap. This is
54 accomplished by observing PMCs below the spacecraft at multiple angles and determining the
55 angular dependence of the cloud brightness against the background Rayleigh scattered sunlight
56 background. AIM was launched on April 25, 2007 and routine observations by CIPS began on
57 May 24, 2007. At this time, AIM has observed one full Northern (2007) and most of the Southern
58 (2007 / 2008) PMC season. Since the purpose of this paper is primarily to describe a technique
59 for obtaining phase functions, we will focus on only a few orbits. In a future work we will
60 describe the morphology of PMC phase functions and compare the obtained phase functions in
61 the northern and southern hemispheres. For now, we describe the algorithm for isolating the
62 PMC brightness from the Rayleigh background and for obtaining the phase functions.

63 **2.0 Observations**

64 The goals of the CIPS instrument are described in this issue by Rusch et al. [2008]. The details of
65 the instrument design and its implantation on AIM are also described in this issue by McClintock
66 et al. [2008]. See also Russell et al. [2008] for the objective of the AIM mission and the other
67 instruments. Here only a brief description and list of the relevant CIPS details are presented.
68 CIPS consists of an array of four cameras operating with a 15 nm passband centered at 265 nm.
69 Each camera has an overlapping FOV and a spatial resolution (at the nadir) of 1 x 2 km. The
70 FOV of the camera system is $80^\circ \times 120^\circ$, centered at the sub-satellite point, with the 120° axis
71 along the orbit track. Because of slant viewing, the spatial resolution increases to 6.4 km near
72 the edge of the FOV of the forward and aft cameras. The combination of images from the four
73 cameras is referred to as a scene. CIPS records scenes of atmospheric and cloud radiance in the
74 summer hemisphere from the terminator to $\sim 40^\circ$ latitude over the sunlit portion of the orbit.

75 Each camera has a focal ratio of 1.12, a focal length of 28 mm, and a 25 mm lens diameter and

76 includes an interference filter and a Charge Coupled Device (CCD) detector system. The
77 throughput of the optical elements and their sizes are designed for a $\pm 1\%$ measurement precision
78 of the background sunlit Earth. The CCD detectors are coupled with image intensifiers and have
79 2048 x 2048 useful pixels that are electronically binned in 4 x 8 combinations for an effective
80 340 (cross track) x 170 (along track) pixel images. The instantaneous field-of-view of an
81 effective picture element is 1 x 2 km projected at the cloud height of 83 km. On average, 26
82 images are produced per orbit in the summer polar region with special 'first light' images just
83 beyond the terminator.

84 Imaging is achieved with this body-fixed camera assembly using an exposure time of 1 second.
85 Scenes are obtained at a cadence of one per 43 seconds. This fact combined with the large field
86 encompassed by a scene results in between four and seven exposures of the same spatial element
87 for each satellite overpass. Each of these observations of the same spatial elements is made at a
88 different scattering and observation angle. The scattering angle, Θ , is the angle between the
89 unscattered photon path and the new path after the scattering. The observation angle, ϕ , is the
90 angle between the zenith and the CIPS line of site (from the ice perspective). In this paper, we
91 refer to the variation of the observed albedo as a function of scattering angle (or observation
92 angle) as a scattering profile. Note that all symbols used in this paper are defined in the
93 Appendix.

94 The range of scattering angles over which an individual location is observed varies along the
95 orbit. At high solar zenith angles, close to the terminator, a nadir observation is near $\Theta = 90^\circ$.
96 Thus observations sunward of nadir yield forward scattered observations ($\Theta < 90^\circ$ and
97 observations anti-sunward produce backward scattered observations ($\Theta > 90^\circ$). As the satellite
98 moves along the orbit to the subsolar point, nadir observations are at $\Theta = 180^\circ$ and observations
99 on either side of nadir are such that $90^\circ < \Theta < 180^\circ$. No forward scattered observations can be
100 made by CIPS at the subsolar point.

101 Figure 1 shows the range of scattering angles per scattering profile as a function of solar zenith
 102 angle. The points on this Figure are from Orbit 424 on May 24 but would be similar for any day
 103 of CIPS operation. An observation is identified by a single grey point on this figure (every 4th
 104 observation is plotted). For select locations, the scattering profile is shown using asterisk
 105 connected by solid lines. At high solar zenith angles, approximately half of the observations are
 106 at $\Theta < 90^\circ$ and half are at $\Theta > 90^\circ$. At progressively lower solar zenith angles, a larger fraction of
 107 the observations are made at $\Theta > 90^\circ$.

108 **3.0 Sources of Observed Radiance**

109 The radiance observed by CIPS is due to two sources. The first is scattered solar radiance due to
 110 ice crystals in PMCs. PMCs are present throughout the summer polar region. The second, ever
 111 present, source is singly-scattered solar radiance due to Rayleigh scattering by atmospheric
 112 molecules. Even for the brightest PMCs, Rayleigh scattering is the dominant source of radiance.
 113 In this section we describe analytic representations of both sources. These analytic expressions
 114 will serve as the basis for the retrievals discussed in the following section.

115 Throughout this work and in general for all CIPS products, radiances are expressed in albedo, the
 116 ratio of atmospheric radiance to solar irradiance. The calculation of albedo from CIPS
 117 observations is discussed in both Rusch et al. [2008] and McClintock et al. [2008]. The units of
 118 albedo are sr^{-1} . We use the symbol G to refer to albedo units of 10^{-6}sr^{-1} .

119 We write the observed albedo due to PMC ice, A_{ice} , as

$$120 \quad A_{ice} = \frac{A_{PMC} P_{ice}}{\cos(\phi)} \quad (1)$$

121 We define the albedo of a PMC, A_{PMC} , as the albedo which would be observed at $\Theta = 90^\circ$. A_{PMC}
 122 contains information about the ice column density, particle size and shape, and index of
 123 refraction. P_{ice} is the ice scattering phase function. With the definitions used here, this phase

124 function is normalized to unity at $\Theta = 90^\circ$. The $\cos(\phi)$ factor corrects for slant path geometry
 125 when viewing the cloud off nadir.

126 The non-cloud brightness is due to Rayleigh scattering of sun light from N_2 and O_2 molecules. At
 127 265 nm, the observed brightness is due to a single scattering and is strongly controlled by ozone
 128 absorption along the path. This wavelength was chosen for CIPS because it is near this
 129 wavelength that ozone absorption peaks and thus provides the greatest contrast between
 130 atmospheric and PMC brightness. Calculations of the limb brightness for similar wavelengths are
 131 discussed by Merkel et al. [2001] for limb geometries and McPeters [1980] for nadir geometries.
 132 At most solar zenith angles, the peak contribution to the observed nadir viewing 265 nm
 133 Rayleigh brightness is from 50 to 55 km. Near 90° solar zenith angle, this altitude rapidly
 134 increases to 65 km.

135 In order to describe the atmospheric albedo due to Rayleigh scattering analytically, we generalize
 136 the result of McPeters [1980]. They provided an analytic result for single scattering, neglecting
 137 attenuation along the path by Rayleigh scattering, and assuming that the ratio of the ozone scale
 138 height to the atmospheric scale height, σ , was constant. We generalize their result to allow for
 139 off-nadir viewing as

$$140 \quad A_{Ray} = \frac{P_{Ray}(\Theta)\Gamma(\sigma+1)\beta N(z_0)}{\mu_V \left(\frac{1}{\mu_V} + \frac{1}{\mu_Z} \right)^\sigma \alpha^\sigma C(z_0)^\sigma} \quad (2)$$

141 where $P_{Ray}(\Theta)$ is the known Rayleigh phase function, Γ is the Gamma function, β is the cross
 142 section for Rayleigh scattering, α is the cross section for pure absorption by ozone, N is the
 143 column density of atmospheric molecules above a reference altitude, z_0 , and C is the column
 144 density of ozone molecules above that reference altitude. A full derivation of Equation 2 is
 145 provided in the appendix. The factors μ_V and μ_Z are path-length factors that account for the slant

146 path through atmospheric layers. For vertical paths their value is unity. As CIPS views off nadir
 147 such that the ϕ increases from zero, μ_V varies as $\cos(\phi)$. Similarly as the solar zenith angle, θ ,
 148 increases, the path-length factor initially varies as $\cos(\theta)$. For θ larger than 80° , a cosine
 149 approximation is inadequate and a Chapman function correction [Chapman, 1931] must be
 150 applied. See Fitzmaurice [1964] for an implementation of the Chapman function. We specify the
 151 solar zenith angle for each scattering profile as that solar zenith angle appropriate to the altitude
 152 of peak Rayleigh contribution, typically near 55 km.

153 Although the reference altitude, z_0 , appears in Equation 2, the equation does not depend directly
 154 on altitude. The column densities must however be consistently referenced to a particular altitude
 155 which we label z_0 . In our applications, we specify an air column density, N , of $2.4 \times 10^{22} \text{ cm}^{-2}$
 156 which occurs near 50 km [Hedin et al., 1986]. This means that any ozone column density
 157 obtained from CIPS observations and the algorithms presented here (unless otherwise corrected)
 158 is the number of molecules in a vertical column above the altitude at which the vertical column
 159 density of air molecules is $2.4 \times 10^{22} \text{ cm}^{-2}$. We adopt an ozone absorption cross section at 265 nm
 160 of $9.261 \times 10^{-18} \text{ cm}^2$ and a Rayleigh scattering cross section of $9.708 \times 10^{-26} \text{ cm}^2$ [Bates, 1984].

161 **4.0 Cloud-Free Radiance**

162 Equation 2 possesses very useful properties. We arrange Equation 2 to place the geometry factors
 163 on one side and the geometry dependant factors on the other. Defining Y and X as

$$164 \quad Y = \log\left(\frac{1}{\mu_V} + \frac{1}{\mu_Z}\right) \quad (3)$$

165 and

$$166 \quad X = \log\left(\frac{A_{Ray} \mu_V}{P_{Ray}(\Theta)}\right). \quad (4)$$

167 It is easily shown that

168

$$Y = -\sigma X + \text{constant. (5)}$$

169 Thus from an observed scattering profile, the slope of the line formed by Y versus X yields the
170 negative of σ . With σ obtained, one can use Equation 2 to solve for C. We refer to this as an
171 “analytic retrieval” for C and σ . It is a rapid and powerful method for analyzing a scattering
172 profile that is thought not to contain radiance from PMCs.

173 We demonstrate the validity of Equations 2 through 5 by examining observations on a CIPS orbit
174 that shows no evidence of PMCs. Orbit 424 from May 24, 2007 is such an orbit. There is no
175 structure or behavior in the CIPS images for that day that suggests the presence of any PMC
176 radiance. We use this orbit then as a baseline cloud-free orbit. Figure 2 shows scattering profiles
177 and Y versus X plots for typical observations near 60°, 70°, 80°, and 90° solar zenith angle. In all
178 cases Y shows a good linear relationship with X. The values of C and σ that are obtained from
179 the intercept and slope of this line are used in Equation 2 to provide a model scattering profile
180 that is compared with the observations. The agreement is excellent. For solar zenith angles $\leq 90^\circ$
181 we have found that model scattering profiles calculated from inferred C and σ reproduce
182 observed cloud-free scattering profiles to within 2% (and typically less than 1%) for any viewing
183 or scattering angle. This value is at about the level of the random noise of the CIPS observations
184 and so we conclude that Equations 2 through 5 describe the cloud-free observations very well
185 and are adequate for use in CIPS data analysis as descriptions of the Rayleigh component to an
186 observed CIPS scattering profile.

187 An indicator of cloud presence may be defined by looking for deviations from the linear
188 relationship of Equation 5. Because ice radiance is heavily forward scattered [Bailey et al., 2007;
189 Rusch et al., 2008], the departure from Equation 5 will be most evident at small scattering
190 angles. There are many possible definitions for a cloud indicator that take advantage of this fact.
191 We have found the following to provide the best results. For each scattering profile, we calculate
192 a slope for Y versus X from observations with scattering angles less than 90° and also from

193 observations with scattering angles greater than 90° . We then divide each group of observations
194 by the appropriate linear fit. For perfect observations all of the resulting values would be unity.
195 We take the mean of the forward scattered results and divide by the mean of the backward
196 scattered results. For cloud-free observations, this value should be very near unity. Where clouds
197 are present, the forward scattered values will be most affected and the resulting ratio will be less
198 than one. We refer to this ratio as RATALL.

199 Figure 3 shows the distribution of values of RATALL for all scattering profiles in Orbit 424
200 between solar zenith angles of 60° and 90° . The distribution is symmetric about unity with a
201 standard deviation of 0.015. This distribution is exactly as would be expected for cloud free
202 observations with random noise corresponding to the CIPS sensitivity. Figure 3 also shows the
203 same distributions for two other orbits, 684 on June 10, 2007 and 1113 on July 9, 2007, where
204 clouds are expected to be present. These orbits were selected because Orbit 684 is representative
205 of an orbit containing many patches of clouds of average (according to CIPS) brightness while
206 Orbit 1113 is one of the orbits with the most and brightest clouds that have been observed by
207 CIPS. The presence of PMCs are easily seen in this distribution by the populations of RATALL
208 values lower than 1.0 and outside the lower side of the orbit 424 distribution. Two standard
209 deviations below the mean of 1.0 for Orbit 424 is the value 0.995. We assume any scattering
210 profile with a RATALL value less than 0.995 should be flagged as likely to contain a PMC
211 signature.

212 **5.0 Retrieval Method**

213 The most crucial step in obtaining PMC properties from CIPS data is separating the ice and
214 Rayleigh scattering contributions. In this section we describe a process for performing that
215 separation. From the above discussion, we have a general description for all CIPS observed
216 scattering profiles

$$217 \quad A_{CIPS} = A_{Ray} + A_{ice} \cdot \quad (6)$$

218 There are four unknowns in Equation 6: C , σ , A_{PMC} , and P_{ice} . The ice phase function, P_{ice} , is
219 dependent upon the mean particle size and shape, the shape of the distribution of particles sizes,
220 and the width of that distribution. In order to minimize the number of unknowns in our analysis,
221 we assume the particles are oblate spheroids with an axial ratio of 2 [Eremenko et al., 2005;
222 Hervig et al., 2008] and have a Gaussian distribution with a width of 14 nm [Rapp and Thomas,
223 2006]. This reduces the description of P_{ice} to a single free parameter, the mean particle size or
224 mode radius, R_m . We then use numerical representations of P_{ice} for these assumptions and R from
225 0 to 300 nm created from the T-matrix model of Mishchenko and Travis [1998]. We emphasize
226 that the stated assumptions are used only to separate the Rayleigh and ice components of the
227 observed radiance and to obtain the ice phase function. Any subsequent interpretation of the
228 retrieved phase function does not require these assumptions. This point will be clarified later.

229 For all locations that meet the $\text{RATALL} < 0.995$ criteria and when CIPS obtains at least 7
230 observations including at least two points with scattering angles less than 90° , the following
231 process is performed. A non-linear least-squares fit is performed to solve Equation 6 for the
232 unknowns C , σ , A_{PMC} , and R_m . While 7 unique observations are nominally sufficient to
233 determine 4 unknowns, we have found that providing constraints on C and σ greatly improves
234 the results. There are numerous methods for obtaining suitable constraints. For example one
235 could find the distributions of C and σ from cloud free observations ($\text{RATALL} > 0.995$) using the
236 analytic retrieval and constrain the retrieved C and σ to be within 2 standard deviations of the
237 mean cloud-free C and σ . We have found however that approximate values for C and σ can be
238 obtained from each scattering profile directly even in the presence of a PMC. Because the ice
239 scattering phase functions are so strongly peaked, PMCs generally contribute very little radiance
240 for scattering angles $\geq 120^\circ$. Through simulations, we have found that performing an analytic
241 retrieval on scattering profiles including only observations at scattering angles greater than 120°
242 yields C and σ results that are never different from the true C and σ by more than 12% (3

243 standard deviations) even for bright clouds. This result changes only negligibly depending on the
244 assumption of the particle distribution. For the clouds that are brighter than 50 G, this assumption
245 has little effect because the errors induced in the Rayleigh component of the scattering profile are
246 small compared to the ice component. The non-linear least-squares fit is performed using the
247 MPFIT routine in the IDL language that is publically available in the SOLARSOFT data analysis
248 package [Freeland and Bently, 2000]. This routine is an implementation of the Levenberg-
249 Marquardt method [Levenberg, 1944; Marquardt, 1963] commonly used in the solar radiance
250 community [e.g. Rodgers et al. 2006].

251 Once the four parameters are obtained, the Rayleigh component of the scattering profile is
252 calculated from Equation 2 and removed to yield A_{ice} . As mentioned previously, we refer to A_{PMC}
253 as the albedo observed at $\Theta = 90^\circ$ and the phase function is then unity at that angle. There is
254 nothing in the above procedure that enforces this result, although the retrieved values at 90° are
255 typically within the range 0.8 to 1.2. We determine the scaling factor to A_{PMC} which normalizes
256 the P_{ice} to 1.0 at 90 scattering angle and adjust A_{PMC} and P_{ice} accordingly.

257 Figure 4 illustrates the process described above. Sample retrievals are shown for scattering
258 profiles containing both a 10G and a 50G PMC from Orbit 1113. The observed albedos are
259 shown as symbols while the retrieved Rayleigh and PMC components of the scattering profile
260 are shown as dashed and dotted lines. The sum of these components is shown as a solid line and
261 overlays the observations very well. Figure 4 shows how the PMC has little affect on the
262 observations for $\Theta > 120^\circ$ as mentioned above.

263 **6.0 Results**

264 The procedure outlined in Section 5 is applied to Orbits 684 and 1113. Before we examine the
265 retrieved phase functions, we plot in Figure 5 the retrieved cloud albedos as a function of solar
266 zenith angle. The albedos are in the range of 0 to 50 G. This range of brightness is greater than
267 that of PMC albedos reported by a long time series of SBUV experiments [Deland et al., 2003;

268 2007]; however, their resolution is 150 x 150 km at cloud height, compared with that of CIPS (5
269 x 5 km). The comparison of PMC albedoes, binned to the coarser resolution of SBUV/2 on
270 NOAA-17 shows an overall agreement to within $\pm 10\%$ [Benze et al, this issue, 2008]

271 Before we can discuss the retrieved phase functions, it is important to assess the reasonableness
272 of the separation of the PMC and Rayleigh components of the observed albedos. In order to do
273 this, we examine calculated values of the nadir viewing Rayleigh albedo. We compare values of
274 this quantity obtained from analytic retrievals of C and σ in locations where there are no PMC to
275 a similar calculation with C and σ obtained from the non-linear least-squares fit at locations
276 where a PMC is present. The presence or non-presence of a PMC is indicated by RATALL as
277 described above. The comparison is made for locations in bins of 1° of solar zenith angle. We use
278 the nadir viewing Rayleigh brightness because it allows us to compare results from scattering
279 profiles obtained at different locations and different observation angles. If at one solar zenith
280 angle, we get similar results for the Rayleigh albedo obtained from different techniques and with
281 and without the presence of a PMC, then the technique is valid. The only assumption is that
282 ozone does not vary appreciably between locations at the same solar zenith angle (or essentially
283 latitude). If this assumption is not valid, then we will obtain a poor comparison between the two
284 sets of results. The nadir viewing Rayleigh albedo is calculated with Equation 2 by setting $\phi = 0^\circ$
285 ($\mu_V = 1$).

286 This comparison is shown in two ways in Figure 5. Figure 5a is for Orbit 684 and Figure 5b is
287 for Orbit 1113. The calculated nadir viewing Rayleigh albedos are shown as dark dots for
288 locations with no PMC present and light dots for locations where a PMC is present. The overlap
289 of the two populations as a function of solar zenith angle shows that the agreement is very good.
290 To get a better understanding of the differences, at each solar zenith angle we calculate the mean
291 nadir albedo for each population and take the ratio. This ratio is plotted in Figure 5 as a function
292 of solar zenith angle using asterisks. A solid line shows a constant value of 1.0 which would

293 indicate perfect agreement. The surrounding dotted lines are $\pm 2.5\%$ of 1.0. Figures 5a and 5b
294 show that the mean differences between the retrieved albedos for the two populations are within
295 2.5% for most solar zenith angles. The differences exceed this value only for very high solar
296 zenith angles where the Rayleigh albedo is weak. To give a feel for the reasonableness of
297 agreement within 2.5%, we note that a 10 G PMC superimposed upon a 100 G Rayleigh
298 background will have about a 25% random uncertainty in its albedo. The exact uncertainty varies
299 with solar zenith angle but this is a good average. As shown in Figure 5a and especially in Figure
300 5b, there are many clouds with albedos brighter than 10G and so have smaller uncertainties.

301 Figure 6 plots all the phase functions obtained between 60° and 90° solar zenith angle for PMC
302 with A_{PMC} within 1 G of 10, 20, 30, and 40 G. The panels also list the mean value of R_m , 53 ± 15
303 nm, 59 ± 10 nm, 56 ± 18 nm, and 55 ± 7 nm respectively obtained for each of these sets of
304 PMCs. Figure 6 also plots the theoretical curves for the T-matrix phase functions for the
305 assumptions listed in Section 5 for the mean value of R_m as well as R_m plus and minus one
306 standard deviation. The shape of the retrieved phase functions is generally very similar to the T-
307 matrix functions. While numerical representations of the phase functions are required by the
308 algorithms, there is nothing in the process that forces the results to look similar to the
309 representative functions.

310 Figure 6 shows that there is much more variability in the phase functions, and therefore the
311 particle sizes, for the dimmer clouds. As the cloud albedo increases, the phase functions become
312 more consistent. Some of the variability in the 10 G phase functions is due to the larger
313 uncertainties due to the lower brightness, but as stated above the average uncertainty for
314 individual albedo observations of this brightness is about 25% and so a significant portion of the
315 noise must also be geophysical. It should be remembered that while the observed brightness of a
316 PMC is typically dominated by the size of the particles and the observing geometry, all geometry
317 factors including those depending on particle size are removed in our retrieved A_{PMC} and so this

318 value is primarily dependent upon ice number density. Figure 6 suggests that when ice densities
319 are at their lowest, perhaps either early or late in the their lifetime, PMC show the largest
320 variability in particle sizes, but when PMC are at their peak in ice densities, the particle sizes
321 tend to stabilize.

322 It should be emphasized that these values of particle mode radius, R_m , are valid for the
323 assumptions of the particle distribution listed in Section 5. The phase functions could be
324 interpreted with other assumptions and different values of R_m would be obtained. We could have
325 also used a different set of assumptions in the retrieval stage, this again would yield a different
326 value of R but there would be little impact on the phase functions themselves. For example, we
327 performed the retrieval using phase functions for spherical particles with the same Gaussian
328 distribution width used for the oblate particles. The retrieved R_m values were different, but the
329 retrieved phase functions were not different at any scattering angle to better than 2%. The
330 conclusion is that CIPS can do an excellent job of retrieving the phase function of the observed
331 PMC ice, but the interpretation of those phase functions to yield particle sizes is dependent upon
332 assumptions made.

333 **7.0 Summary and Conclusions**

334 We have developed an algorithm that uses the CIPS data to retrieve values of PMC albedo and
335 phase functions. The CIPS absolute albedo measurements have been shown to be consistent with
336 those measured by the well calibrated SBUV instruments [Benze et al. 2008, this issue]. The
337 results for particle phase functions and albedo, under the assumptions discussed in Sections 5
338 and 6, are very reasonable and compare favorably with models [Rapp and Thomas, 2006] and
339 other measurements [Gumbel et al., 2001]. The spatial resolution of the CIPS instrument, 5 km,
340 allows for the detection and derivation of the properties, of thousands of clouds each orbit
341 [McClintock et al. 2008, this issue]. The results for a complete season will provide an
342 unprecedented look at PMC properties including albedo, phase functions, and ice content as a

343 function of time and location.

344 The other AIM remote sensing instrument, SOFIE [Gordley et al., 2008] views the same region
345 of space as CIPS once each orbit. SOFIE results [Hervig et al. 2008, this issue] provide particle
346 properties at this location. Future studies using the combination of SOFIE and CIPS data will
347 take advantage of this unique observational scenario for cross validation and further definition of
348 cloud properties for microphysical studies.

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451

452 **Appendix: Derivation of the C – Sigma Algorithm**

453 Our goal is to provide an analytic description of the Rayleigh brightness with a minimum of free
454 parameters. An overview of the physics of the problem and a relevant figure can be found in
455 Merkel et al. [2001]. At 265 nm, there is only one scattering of sunlight from atmospheric
456 molecules. Photons are removed along the path through absorption by O₃. We neglect attenuation
457 by Rayleigh scattering which is known to yield only a 1% effect [McPeters, 1980].

458 For one infinitesimal altitude level, z , the contribution to the observed intensity is

$$459 \quad dI = dz \frac{n_{air}(z)\beta P_{Ray}(\Theta)F}{\mu_V} \exp\left[-\left(\frac{1}{\mu_V} + \frac{1}{\mu_z}\right)(\tau_\beta + \tau_\alpha)\right]. \quad (A1)$$

460 τ_β , and τ_α are the vertical optical depths due to Rayleigh scattering and pure absorption by ozone,

$$461 \quad \begin{aligned} \tau_\beta(z) &= \beta \int_z^\infty n_{air}(z) dz = N(z)\beta \\ \tau_\alpha(z) &= \alpha \int_z^\infty n_{O_3}(z) dz = X(z)\alpha \end{aligned} \quad (A2)$$

462 $N(z)$ and $X(z)$ are the air and ozone column densities respectively.

463 The observed intensity and therefore the Earth albedo is obtained by the following integral,

$$464 \quad A = \frac{I}{F} = \int_0^\infty d\tau_\beta \frac{P_{Ray}(\Theta)}{\mu_V} \exp\left[-\left(\frac{1}{\mu_V} + \frac{1}{\mu_z}\right)(\tau_\beta + \tau_\alpha)\right]. \quad (A3)$$

465 Letting C be the ozone column density at reference altitude z_0 , the altitude dependent column
466 density of ozone, X , can be written as

$$467 \quad X = C \left(\frac{N}{N_0}\right)^{1/\sigma} \quad (A4)$$

468 where N_0 is the air column density above z_0 ,

$$469 \quad N(z) = N_0 \exp \left[- \int_z^\infty dz' \frac{1}{H_{air}(z')} \right] \quad (A5)$$

470 where H_{air} is the altitude-dependent scale height of air. We define σ as the ratio of the ozone
471 to air scale height,

$$472 \quad \sigma = \frac{H_{ozone}}{H_{air}} \quad (A6)$$

473 We assume that σ is constant with altitude. This does not require that either scale height in
474 Equation A6 is constant, only the ration of the two scale heights.

475 Equation A4 is rewritten in terms of optical depth to show

$$476 \quad \tau_\alpha^\sigma = \tau_{\alpha 0}^\sigma \frac{\tau_\beta}{\tau_{\beta 0}} \quad (A7)$$

477 Ignoring attenuation by Rayleigh scattering as mentioned above, we then rewrite Equation A3 as

$$478 \quad A = P_{Ray}(\Theta) \int_0^\infty \frac{d\tau_\beta}{\mu_V} \exp \left[- \left(\frac{1}{\mu_V} + \frac{1}{\mu_z} \right) (\tau_\alpha) \right] \quad (A8)$$

479 Letting k represent the term in parenthesis,

$$480 \quad A = \frac{P_{Ray}(\Theta)}{\mu_V} \int_0^\infty d\tau_\beta e^{-k\tau_\alpha} \quad (A9)$$

481 which can be rewritten and solved with a Laplace transform,

$$482 \quad \int d\tau_\alpha \frac{d\tau_\beta}{d\tau_\alpha} e^{-k\tau_\alpha} = k \int d\tau_\alpha \tau_\beta(\tau_\alpha) e^{-k\tau_\alpha} \quad (A10)$$

483 which is valid as long as $\tau_\beta(\tau_\alpha)=0$ which is true in this case (all optical depths are zero at the top

484 of the atmosphere). Thus Equation A9 is rewritten as

485
$$A = \frac{P_{Ray}(\Theta)}{\mu_V} \int_0^{\infty} d\tau_{\alpha} \frac{\tau_{\beta_0}}{\tau_{\alpha_0}^{\sigma}} \tau_{\alpha}^{\sigma} e^{-k\tau_{\alpha}} . \quad (A11)$$

486 Through some manipulation and use of the gamma function Equation A11 becomes

487
$$A = \frac{P_{Ray}(\Theta)}{\mu_V} \frac{\tau_{\beta_0}}{\tau_{\alpha_0}^{\sigma}} \left(\frac{1}{k}\right)^{\sigma} \Gamma(\sigma + 1) . \quad (A12)$$

488 Using the definition of k, Equation A12 yields

489
$$A_{Ray} = \frac{P_{Ray}(\Theta)\Gamma(\sigma + 1)\beta N(z_0)}{\mu_V \left(\frac{1}{\mu_V} + \frac{1}{\mu_Z}\right)^{\sigma} \alpha^{\sigma} C(z_0)^{\sigma}} \quad (A13)$$

490 which is Equation 2.

491 **Figure Captions**

492

493 **Figure 1.** Scattering and solar zenith angles for each observation of orbit 424 on May 24,
494 2007 (dots). The 7 observations for 13 individual locations are shown as asterisks
495 connected by solid lines. The 7 observations of albedo form the scattering profile for
496 those locations. Latitudes are shown at the top of the figure.

497

498 **Figure 2.** Representative scattering profiles at 4 solar zenith angles from orbit 424 on May
499 24, 2007 (top row). Circles are for observations at scattering angles less than 90° while
500 squares are observations at scattering angles greater than 90° . The inferred values of C
501 and σ for each scattering profile are listed. In the bottom row, derived values of Y are
502 plotted against the geometry factors X for each of the above scattering profiles. Fitted
503 lines are also shown.

504

505 **Figure 3.** Distribution of RATALL values for Orbits 424, 684, and 1113.

506

507 **Figure 4.** Sample retrievals for scattering profiles containing a 10G (left panel) and a
508 50G (right panel) PMC from Orbit 1113. Points are observed albedo. Circles are for
509 observations at scattering angles less than 90° and squares are observations at
510 scattering angles greater than 90° . Dotted lines with pluses are the retrieved cloud
511 albedo. Dashed lines with pluses are retrieved Rayleigh albedo. The sum of the
512 retrieved cloud and Rayleigh albedos are shown as solid lines.

513

514 **Figure 5a.** Ratio of the nadir viewing Rayleigh albedo as calculated from the retrieved
515 Rayleigh parameters for observations with a PMC present to the same value for
516 observations where no PMC is present. The mean value of this ratio for observations with
517 solar zenith angles within 1° of select solar zenith angles are shown as asterisks. Vertical
518 lines reflect the mean plus and minus one standard deviation. The solid horizontal line
519 shows a constant value of 1.0. The dotted lines are 2.5% above and below 1.0. Dark
520 dots show the retrieved Rayleigh albedo (scaled as shown) for observations where no
521 PMC is detected. Light dots show the retrieved albedo (scaled as shown) inferred from
522 observations where a PMC is detected. Pluses show the retrieved cloud albedos. All
523 values are for orbit 684.

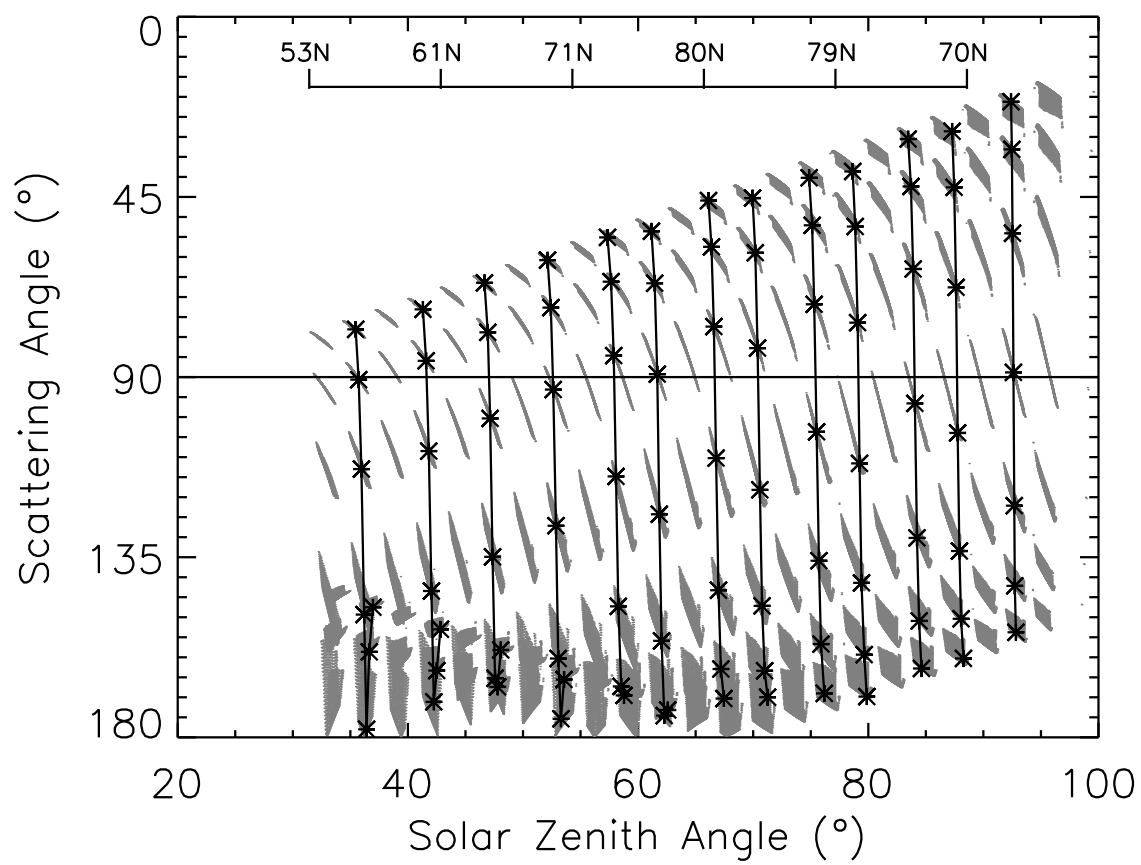
524

525 **Figure 5b.** Same as Figure 5a but for Orbit 1113.

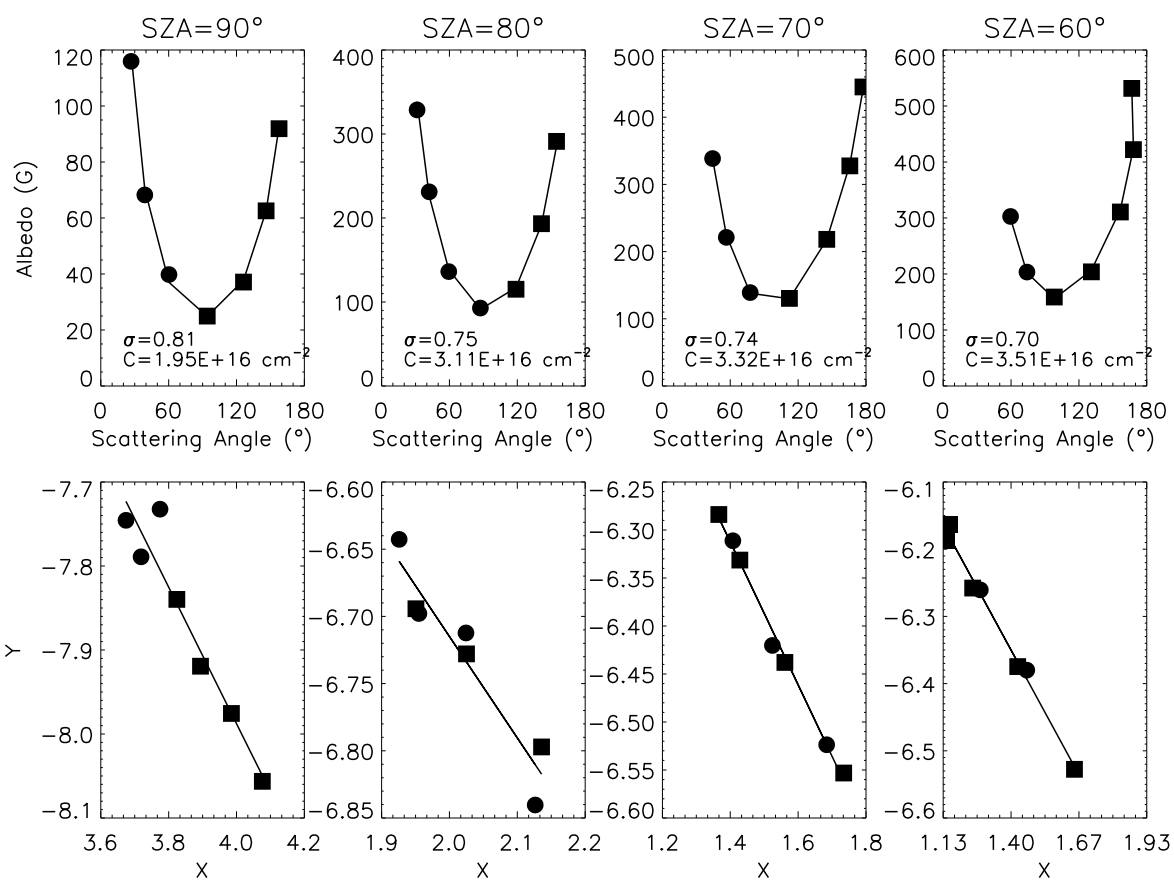
526

527 **Figure 6.** Retrieved phase functions for Orbit 1113 for PMC with albedos within 1G of 10,
528 20, 30, and 40G. Solid lines are theoretical phase functions for the shown mean radius.
529 (See text for assumptions regarding theoretical phase functions). Dotted and dashed
530 lines are theoretical phase functions for the shown mean radius minus and plus the
531 shown standard deviation respectively.

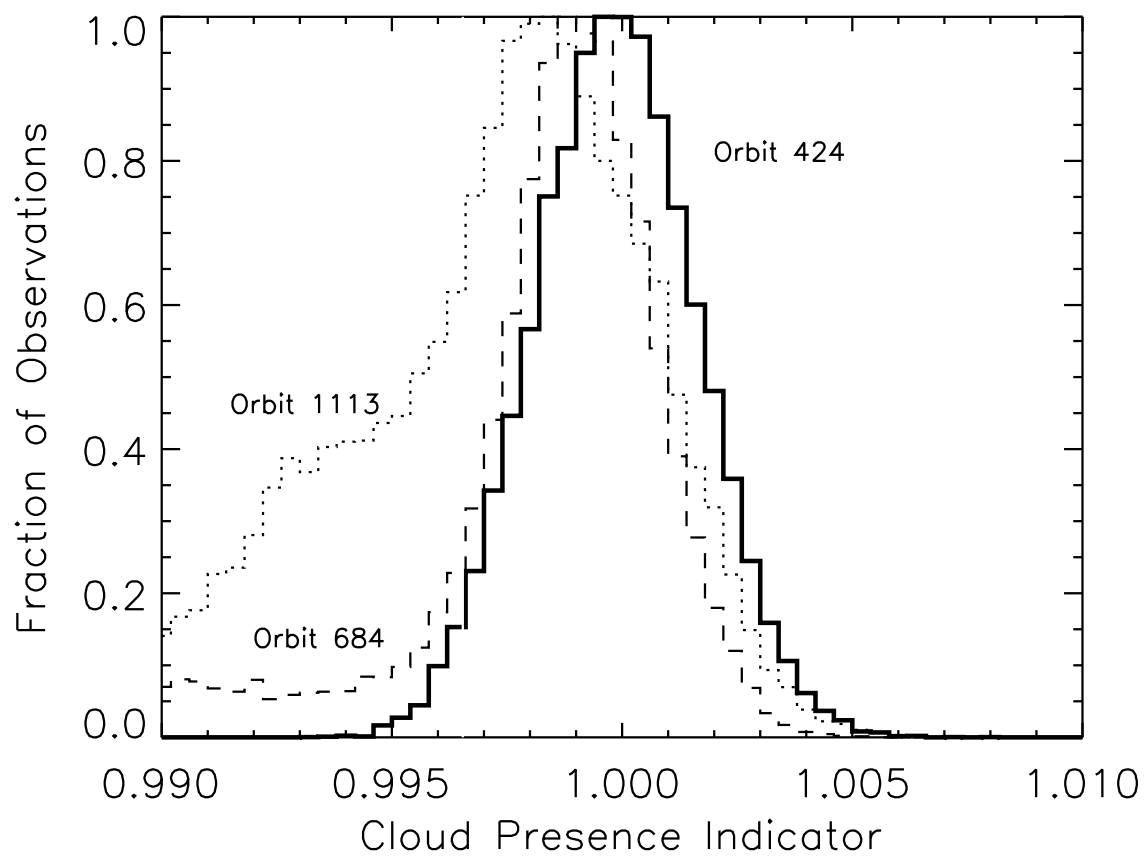
Figure



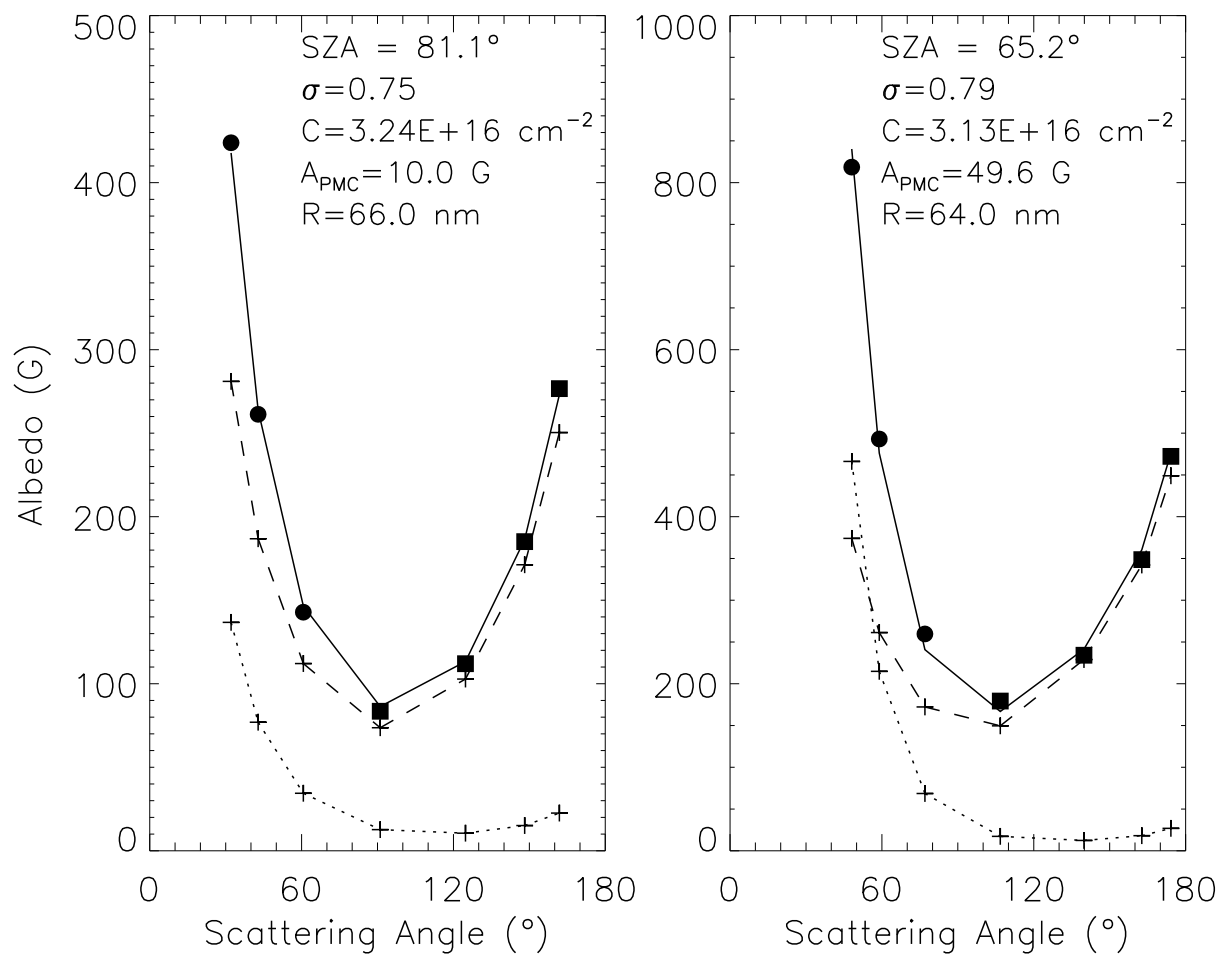
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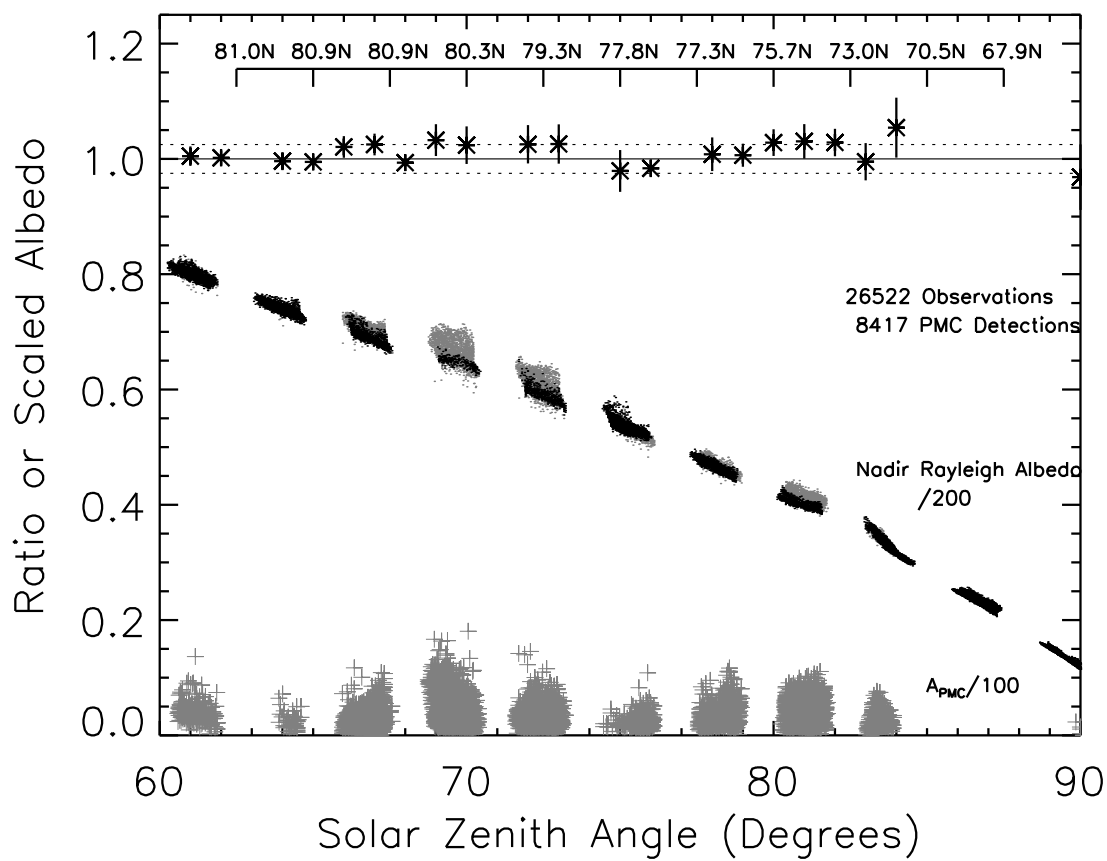
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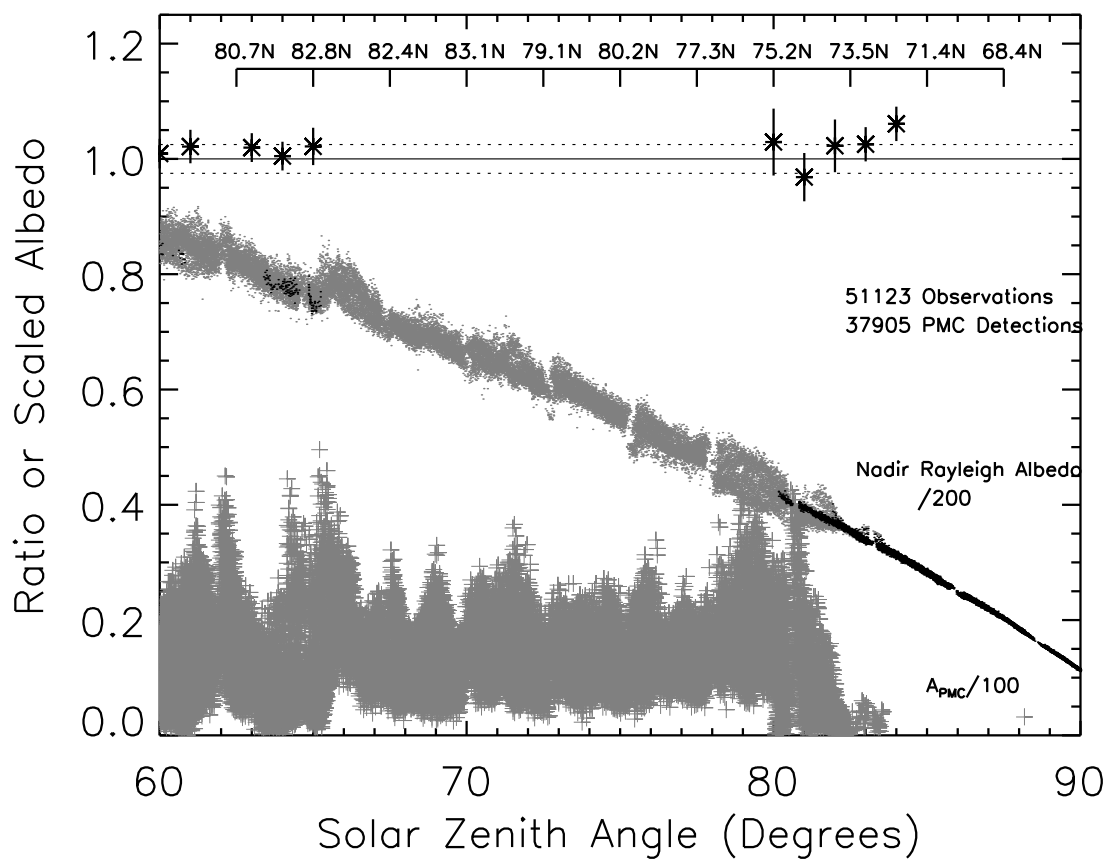
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